Migrations and Fiscal Sustainability

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Labor mobility and fiscal policy in the long run

- Undesirable fiscal consequences of migrations in sending countries:
 - challenge to social security systems (e.g. Storesletten [2000])
 - increase of public debt per capita (e.g. Brunnermeier et al. [2016])
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- Gap in the literature: interactions between the global effects of open borders and country-level fiscal policy

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 - Cons: higher debt \Rightarrow future fiscal problems \Rightarrow lower consumption of future old agents \Rightarrow deters migrants

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 - Cons: financial crisis \Rightarrow lower output \Rightarrow less resources to be redistributed \Rightarrow deters migrants

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 - Pros: higher consumption of old people
 - Cons: higher taxation of workers \Rightarrow consumption of young agents is lower \Rightarrow lower lifetime utility \Rightarrow outflow of workers
 - Moreover, outflow of workers \Rightarrow lower output \Rightarrow potentially lower consumption of old people

Mechanism:

- Fiscal benefits from immigration:
 - larger tax base
 - space for additional debt issuance
- To attract immigrants government raises:
 - worker's disposable income (by cutting labor tax)
 - $\cdot\,$ raises future provision of public goods (by reducing public debt)
- Fiscal prudence lowers global real interest rate
- Thus: private capital rises in each country \Longrightarrow "a rising tide that lifts all boats"

Framework

- **Starting point** the model by Song, Storesletten and Zilibotti [2012]:
 - continuum of countries
 - two overlapping generations
 - production factors: capital and labor
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Our extensions:

- cross-country labor mobility
- country-level productivity shocks
- debt renegotiation

Exercises and Findings

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• comparison of the model with the "EU-like" migrations with a no-migration counterfactual

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• Main findings:

- in the presense of endogenous migrations, governments conduct more prudent fiscal policies
- global effects of migration: lower average Debt-to-GDP ratio (80% vs 72%), lower spreads (1.5% vs 1.2%) and higher output (+1.5%)
- \cdot welfare improvement even for the least productive economies

- Heterogeneous labor markets in currency unions: Dolls et al. [2018], Abraham et al. [2019], Moyen et al. [2019]
- Social security, fiscal policy and migrations: Storesletten [2000], Bandeira et al. [2018]
- Migrations and allocation of resources: Klein and Ventura [2009], Kennan [2013], Tombe and Zhu [2019], Walerych [2020]
- Labor mobility in currency unions (short-run analysis): Farhi and Werning [2014], Hauser and Seneca [2019]
- Migrations, trade and labor heterogeneity: Iranzo and Peri [2009], Giovanni et al. [2015]
- Labor mobility and sovereign default: Alessandria et al. [2019]

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- Financial intermediaries:
 - \cdot trade all types of assets
 - pricing rules of financial contracts

• Maximization problem:

$$U^{y} = \max_{c^{y}, c^{o'}, a'} \log c^{y} + \sigma \cdot \left[\log c^{o'} + \theta^{o} \cdot \mathbb{E} \left(\log g' \right) \right]$$
subject to:
$$c^{y} + a' = (1 - \tau) \cdot w$$
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• Optimal policy rules:

$$\begin{cases} c^{y}\left(\tau,\,w\right) = \frac{1}{1+\sigma}\cdot\left(1-\tau\right)\cdot w\\ a'\left(\tau,\,w\right) = \frac{\sigma}{1+\sigma}\cdot\left(1-\tau\right)\cdot w\\ c^{o'}\left(\tau,\,w\right) = \frac{R^{h}\cdot\sigma}{1+\sigma}\cdot\left(1-\tau\right)\cdot w \end{cases}$$

- \cdot Number of old agents at the beginning of the period: n^o
- Every old agent delivers one young agent
- Survival rate: $\sigma \in (0,1)$

Model: demography, migrations and young agents

- Distribution of lifetime utilities U^y across countries: F
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- $\cdot\,$ Two stages of the individual migrations process:
 - 1. Random search: every young agent draws a migration opportunity $\hat{U^y}$ from the distribution with c.d.f. $\Phi \circ F$ (with $\Phi' > 0, \Phi'' > 0$)
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- \cdot Number of emigrants: E
- Number of immigrants: I
- Number of young agents who live in a given country:

$$n^{y}(n^{o}, U^{y}, F) = n^{o} - E(n^{o}, U^{y}, F) + I(n^{o}, U^{y}, F)$$

- Formulas for *E* and *I*: details
- Net gross migration rate:

$$\eta \equiv \frac{n^y}{n^o}$$

Model: supply side

- $\cdot\,$ Country-level productivity shocks: y
- Debt renegotiation: $d \in [0, 1]$
- Productivity cost of renegotiation: $\chi(d)$ with $\chi' < 0$ and $\chi'' < 0$

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- Productivity cost of renegotiation: $\chi\left(d\right)$ with $\chi^{\prime}<0$ and $\chi^{\prime\prime}<0$
- Firm maximization problem:

$$\max_{K,N} \left(\chi\left(d\right) \cdot y \cdot K^{\alpha} \cdot N^{1-\alpha} - w \cdot N - R^{f} \cdot K \right)$$

- Capital: perfect cross-border mobility, depreciates at rate 100% after one period
- Local labor market clearing: $n^y = N$

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- · Country-level wage:

$$w = (1 - \alpha) \cdot \left(\frac{\alpha}{R^f}\right)^{\frac{\alpha}{1 - \alpha}} \cdot (\chi(d) \cdot y)^{\frac{1}{1 - \alpha}}$$

· Government problem:

$$\max_{\tau,\,b',\,d,\,g}\left\{\alpha^y\cdot U^y+\alpha^o\cdot U^o\right\}$$

subject to:

$$\begin{split} U^{y} &= \log c^{y} \left(\tau, w\left(d, y\right)\right) + \sigma \cdot \log c^{o'} \left(\tau, w\left(d, y\right)\right) + \sigma \cdot \theta^{o} \cdot \mathbb{E} \log \Gamma\left(b', y'\right) \\ U^{o} &= \log c^{o} \left(\tau_{-1}, w_{-1}\right) + \theta^{o} \cdot \log\left(g\right) \\ \underbrace{\sigma \cdot g}_{\text{public spending}} + \underbrace{\left(1 - d\right) \cdot \left(-b\right)}_{\text{outstanding debt}} = \underbrace{\tau \cdot w\left(d, y\right) \cdot \eta\left(U^{y}\right)}_{\text{tax revenues}} + \underbrace{q\left(b', y\right) \cdot \left(-b'\right) \cdot \eta\left(U^{y}\right)}_{\text{issued debt}} \end{split}$$

- Pareto weights α^y and α^o proportional to population sizes

Model: competitive financial intermediaries

- Maximization problem:
 details
- Asset pricing:

$$q(b_{t+1}, y_t) = \frac{1 - \mathbb{E}_{y_{t+1}|y_t} d(b'(b_t, y_t), y_{t+1})}{R}$$
$$\sigma \cdot R^h = R$$
$$R = R^f$$

Model: consistency conditions

• Law of motion of countries across states:

$$\mu'\left(n^{o'},b',y'\right) = \sum_{n^{o},b,y} \left[\pi\left(y'|y\right) \cdot \mathbb{I}_{\left\{\eta\left(U^{y}(b,y),\Omega\right) \cdot n^{o} = n^{o'}\right\}}\right]$$

$$\cdot \mathbb{I}_{\left\{ b'(b,y)=b'\right\} }\cdot \mu \left(n^{o},b,y\right)]$$

- Market clearing for assets:
 details
- Markov Perfect Equilibrium condition:

$$\forall_{b,y} g (b,y) = \Gamma (b,y)$$

• Definition of Stationary Markov Perfect Competitive Equilibrium:



Mechanism: fiscal prudence

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- Basically, governments compete for labor force
- Intratemporal optimality condition of government (between private consumption and government spending):

$$\frac{\partial U^y}{\partial c^y} = \frac{\partial U^o}{\partial g} \cdot (1+\sigma) - \underbrace{\frac{\partial U^o}{\partial g} \cdot \frac{\eta'}{\eta} \cdot \frac{\partial U^y}{\partial c^y} \cdot (\tau \cdot w - q \cdot b')}_{\text{fiscal benefits from immigrants}}$$

• Intertemporal optimality condition of government (between today and tomorrow):

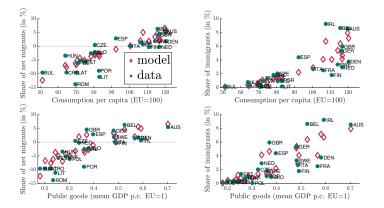
$$\frac{\partial U^y}{\partial b'} = \frac{\partial U^o}{\partial g} \cdot \left(\frac{\partial q}{\partial b'} \cdot b' + q\right) - \underbrace{\frac{\partial U^o}{\partial g} \cdot \frac{\eta'}{\eta} \cdot \frac{\partial U^y}{\partial b'} \cdot (\tau \cdot w - q \cdot b')}_{Q_{ab}}$$

fiscal benefits from immigrants

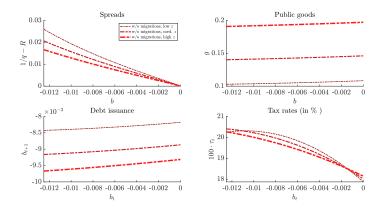
Calibration (for T = 30 years)

Parameter	Description	Value	Calibration target
σ	Survival rate	0.30	Old age dependency ratio
α	Output elasticity of capital	0.33	Standard value in the literature
ρ_T	Persistence of the AR(1) process	0.61	Country-level productivity process
$\sigma_{\epsilon, T}$	Std. error of the AR(1) process	0.08	Country-level productivity process
χ_0	Parameter of defult penalty	0.04	Mean debt to GDP ratio of 72%
χ_1	Parameter of defult penalty	2.10	Mean spread over riskless rate of 1.2%
θ^{o}	Preferences for public goods	1.00	Public goods for the elderly to GDP of 12%
ψ_1	Parameter of matching technology	2.95	Intra-EU migrations
ψ_2	Parameter of matching technology	1.50	Intra-EU migrations
ϕ	Parameter of matching technology	1.40	Intra-EU migrations

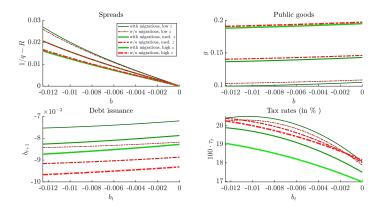
Calibration: matching process



Results: optimal policies at the country level

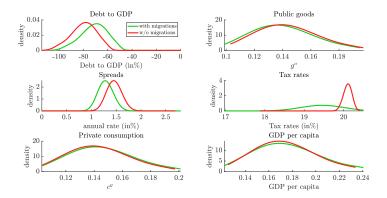


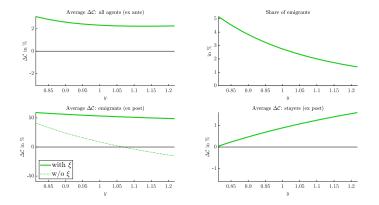
Results: optimal policies at the country level



	w/o migrations	with migrations
Mean debt-to-GDP ratio	80%	72%
Average annual spread	1.5%	1.2%
Aggregate capital	1.00	1.03
Global GDP	0.347	0.352 (+1.5%)

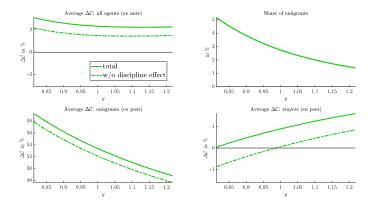
Results: distributions of countries over variables and policies





	w/o migrations	Counterfactual: with Migrations but w/o FP	w/o migrations and with FP
Mean debt-to-GDP ratio	80%	78%	72%
Average annual spread	1.5%	1.4%	1.2%
Aggregate capital	1.00	1.01	1.03
Global GDP	0.347	0.350 (+0.9%)	0.352 (+1.5%)

Results: quantitative role of fiscal prudence 2



Thank you for your attention!

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Formulas for E and I i

Country-level number of emigrants:

$$\begin{split} E\left(n^{o}, U^{y}, F\right) &= n^{o} \cdot \left[\sum_{\hat{B}, \hat{y}, \hat{n^{o}}} \mathbb{P}_{\Phi}\left(U^{y}\left(\hat{n^{o}}, \hat{B}, \hat{y}\right), F\right) \right. \\ &\times \frac{\mu\left(\hat{n^{o}}, \hat{B}, \hat{y}\right) \cdot \hat{n^{o}}}{\sum_{\tilde{B}, \tilde{y}, \tilde{n^{o}}} \mathbb{I}_{\left\{U^{y}\left(\tilde{n^{o}}, \tilde{B}, \hat{y}\right) = U^{y}\left(\hat{n^{o}}, \hat{B}, \hat{y}\right)\right\}} \cdot \mu\left(\tilde{n^{o}}, \tilde{B}, \tilde{y}\right) \cdot \tilde{n^{o}}} \\ &\times \Psi\left(U^{y}\left(\hat{n^{o}}, \hat{B}, \hat{y}\right) - U^{y}\left(n^{o}, B, y\right)\right)\right]. \end{split}$$

Immigrants arriving to the analyzed economy:

$$I\left(n^{o}, U^{y}, F\right) = \sum_{\hat{B}, \hat{y}, \hat{n^{o}}} \left[\mu\left(\hat{n^{o}}, \hat{B}, \hat{y}\right) \cdot \hat{n^{o}} \cdot \mathbb{P}_{\Phi}\left(U^{y}, F\right) \right]$$

Formulas for E and I ii

$$\times \frac{1 \cdot n^{o}}{\sum_{\tilde{B}, \tilde{y}, \tilde{n^{o}}} \mathbb{I}_{\left\{U^{y}\left(\tilde{n^{o}}, \tilde{B}, \tilde{y}\right) = U^{y}\right\}} \cdot \mu\left(\tilde{n^{o}}, \tilde{B}, \tilde{y}\right) \cdot \tilde{n^{o}}} \times \Psi\left(U^{y} - U^{y}\left(\hat{n^{o}}, \hat{B}, \hat{y}\right)\right)\right].$$

where probability $\mathbb{P}_{\Phi}\left(\hat{U^y},F\right)$ of drawing opportunity $\hat{U^y}$ from distribution characterized with c.d.f. $\Phi \circ F$ is:

$$\mathbb{P}_{\Phi}\left(\hat{U^{y}},F\right) = \lim_{\epsilon \to 0} \left\{ \Phi \circ F\left(\hat{U^{y}}+\epsilon\right) - \Phi \circ F\left(\hat{U^{y}}-\epsilon\right) \right\}$$

and the c.d.f. of disutility shock ξ is Ψ .

◀ back

Similar to Chatterjee et al. [2007] (financial intermediaries sell the amount \bar{K}_{t+1} of capital, choose the number A of type (b', y) sovereign loan/deposit contracts at price q and A^P of private loan/deposit contracts signed with households populating a country indexed with (b, y) traded at price q^P , to maximize the discounted sum of profits):

$$\sum_{t=0}^{+\infty} R^{-t} \cdot \Pi_t$$

where:

$$\Pi_{t} = \left(1 - \delta + R^{f}\right) \cdot \bar{K}_{t} - \bar{K}_{t+1}$$
$$+ \sum_{b_{t+1}, y_{t}} q\left(b_{t+1}, y_{t}\right) \cdot A\left(b_{t+1}, y_{t}\right) \cdot b_{t+1} - \sum_{b_{t}, y_{t-1}} \left(1 - d\left(b_{t}, y_{t-1}\right)\right) \cdot A\left(b_{t}, y_{t-1}\right) \cdot b_{t}$$

Intermediary: maximization problem ii

$$+\sum_{b_{t},y_{t}}A^{P}(b_{t},y_{t})\cdot a_{t+1}(b_{t},y_{t})-\sum_{b_{t-1},y_{t-1}}\sigma\cdot R^{h}\cdot A^{P}(b_{t-1},y_{t-1})\cdot a_{t}(b_{t-1},y_{t-1})\cdot a_{t}(b_{t-1},$$



Market clearing condition: asset market i

Consistency condition for private contracts:

$$A^{P}\left(b,y\right) = \sum_{b,y,n^{o}} \eta\left(U^{y}\left(b,y\right)\right) \cdot n^{o} \cdot \mu\left(n^{o},b,y\right)$$

Consistency for sovereign debt contracts:

$$A\left(b',y\right) = \sum_{b,y,n^{o}} \mathbb{I}_{\left\{b'\left(b,y\right)=b'\right\}} \cdot \eta\left(U^{y}\left(b,y\right)\right) \cdot n^{o} \cdot \mu\left(n^{o},b,y\right)$$

Market clearing condition for assets:

$$\bar{K}_{t+1} - \sum_{b_{t+1}, y_t} q\left(b_{t+1}, y_t\right) \cdot A\left(b_{t+1}, y_t\right) \cdot b_{t+1} - \sum_{b_t, y_t} A^P\left(b_t, y_t\right) \cdot a_{t+1}\left(b_t, y_t\right) = 0$$



Definition: A Stationary Markov Perfect Competitive Equilibrium (SMPCE) consists of prices R, R^f , R^h , debt contracts q(b', y), wages w, household policies c^y , $c^{o'}$, a', government policies τ , d, b', g, choices of financial intermediaries A, A^P , \bar{K}' , distribution μ^* and function η , such that:

1. Policies c^y , $c^{o'}$, a' solve household problem given au, g', R^h and w,

2. Policies τ , d, b', g solve government's problem given Γ , w, q, η ,

3. First order conditions associated with financial intermediaries problem hold

- 4. Markov Perfect Equilibrium condition holds
- 5. Consistency conditions hold
- 6. Pareto weights satisfy $\alpha^y = \eta$ and $\alpha^o = \sigma$

