Financial Vulnerability and Monetary Policy

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Introduction

Financial Vulnerability and Monetary Policy

Financial vulnerability: Amplification mechanisms in the financial sector

Two questions are hotly debated

1. Does monetary policy impact the degree of financial vulnerability?

2. Should monetary policy take financial vulnerability into account?

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Financial Variables Predict Tail of Output Gap Distribution

Based on "Vulnerable Growth" by Adrian, Boyarchenko and Giannone (AER, 2018)



Conditional Mean-Volatility Line for Output Gap Growth



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Conditional Mean-Volatility Relation for Inflation



Patterns Hold in Panel of Countries



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Overview of Microfounded Non-Linear Model

- Firm optimization gives standard New Keynesian Phillips Curve
- Households are as in New Keynesian model but
 - Cannot finance firms directly
 - Can trade any financial assets (stocks, riskless desposits, etc.) with banks
- Banks
 - Finance firms
 - Trade financial assets among themselves and with households
 - Have a preference (risk aversion) shock
 - Subject to Value-at-Risk constraint
- Financial markets are complete but prices are distorted

Price of Risk and No Arbitrage

- Single source of risk: Browninan motion Z_t
- Real risk-free rate is R_t
- ▶ A state price density (SPD) is a process with $Q_0 \equiv 1$ and

$$\frac{dQ_t}{Q_t} \equiv -R_t dt - \eta_t dZ_t$$

such that for all assets j

$$S_{j,t} = \frac{1}{Q_t} \mathbb{E}_t \left[\int_t^\infty Q_s D_{j,s} ds \right]$$

where η_t is the "market price of risk"

• Expected excess returns μ_t , volatility σ_t and $\eta_t = \sigma_t^{-1} \mu_t$

The Intermediation Sector Setup

Each "bank" solves a standard Merton portfolio choice problem augmented by a Value-at-Risk constraint and preference shocks

$$V(X_t) = \max_{\{\theta_t, \delta_t\}} \mathbb{E}_t \left[\int_t^\infty e^{-\beta(u-t)} e^{\zeta_u} \log(\delta_u X_u) du \right]$$

$$s.t.$$

$$\frac{dX_t}{X_t} = (R_t - \delta_t + \theta_t \mu_t) dt + \theta_t \sigma_t dZ_t$$

$$VaR_{\tau,\alpha}(X_t) \leq a_V X_t$$

$$d\zeta_t = -\frac{1}{2} s_t^2 dt - s_t dZ_t$$

$$ds_t = -\kappa(s_t - \bar{s}) + \sigma_s dZ_t$$

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Intermediation Sector

The Intermediation Sector Setup

$$V(X_{t},t) = \max_{\{\theta_{t},\delta_{t}\}} \mathbb{E}_{t}^{bank} \left[\int_{t}^{\infty} e^{-\beta(u-t)} \log(\delta_{u}X_{u}) du \right]$$

s.t.
$$\frac{dX_{t}}{X_{t}} = (R_{t} - \delta_{t} + \theta_{t}\mu_{t} - \theta_{t}\sigma_{t}s_{t}) dt + \theta_{t}\sigma_{t}dZ_{t}^{s}$$

$$VaR_{\tau,\alpha}(X_{t}) \leq a_{V}X_{t}$$

$$ds_{t} = -\kappa(s_{t} - \bar{s}) + \sigma_{s}dZ_{t}^{s}$$

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The Banks' VaR Constraint and Amplification

- ▶ Let $\hat{X_t}$ be projected wealth with fixed portfolio weights from t to $t + \tau$
- ► $VaR_{\tau,\alpha}(X_t)$ is the α^{th} quantile of the distribution of $\hat{X}_{t+\tau}$ conditional on time-*t* information



Optimal Portfolio and Dividends

The optimal portfolio is characterized by

$$\theta_t = \frac{1}{\gamma_t} (\mu_t / \sigma_t^2 - s_t / \sigma_t)$$
$$\delta_t = u(\gamma_t)\beta$$

 $\gamma_t \in (1,\infty)$ such that: $VaR_{ au,lpha}\left(X_t
ight) = X_ta_V$

or $\gamma_t ~=~ 1$ if VaR does not bind

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State-Price Density of Intermediaries

• Lagrange multiplier of VaR is increasing in η_t and γ_t

$$\lambda_{VaR,t} = G(\eta_t, \gamma_t, s_t)$$

The marginal value of one unit of wealth is

$$Q_t^{bank} = e^{\zeta_t} e^{-\beta t} \left(\delta_t X_t \right)^{-1} \left(1 - \lambda_{VaR,t} \right)$$
$$= e^{\zeta_t} e^{-\beta t} \left(\delta_t X_t \right)^{-1} \left(1 - G(\eta_t, \gamma_t, \mathbf{s}_t) \right)$$

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Representative Household

Household solves

$$\max_{\{C_t, N_t, \omega_t\}} \mathbb{E}_t \left[\int_t^\infty e^{-\beta(u-t)} \left(\frac{C_u^{1-\sigma}}{1-\sigma} - \frac{N_u^{1+\varsigma}}{1+\varsigma} \right) du \right]$$

subject to

$$d(P_tF_t) = W_tN_tdt - P_tC_tdt + \omega_td(P_tS_t)$$
$$\omega_{goods,t} = 0$$

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Equilibrium price of risk

Households and Intermediaries Agree on Pricing

The household's SPD is

$$Q_t^{house} = e^{-\beta t} C_t^{-\gamma}$$

• The household's Euler equation and market clearing $(C_t = Y_t)$ give the IS equation

$$d \log Y_t = \frac{1}{\gamma} \left(i_t - \pi_t - \beta + \frac{1}{2} \eta_t^2 \right) dt + \frac{\eta_t}{\gamma} dZ_t$$

where i_t is the nominal interest rate

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Households and Intermediaries Agree on Pricing

- Banks and households trading in complete markets means marginal utilities agree Q_t^{house} = Q_t^{bank}
- Matching the volatility of Q_t^{house} and Q_t^{bank}

$$\eta_t = \eta(\gamma_t, s_t) = \eta(V_t, s_t)$$

where

$$V_t \equiv VaR_{\tau,\alpha}(dy_t)$$

= $-\tau \mathbb{E}_t[dy_t/dt] - \mathcal{N}^{-1}(\alpha)\sqrt{\tau} Vol_t(dy_t/dt)$

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Power of Continuous Time

- Can solve banks' VaR problem in closed form (even if markets were incomplete)
- Linearizing drift and stochastic parts retains time variation in risk premium

$$dy_t = \frac{1}{\gamma} (i_t - r - \pi_t) dt + \xi (V_t - s_t) dZ_t$$
$$V_t = -\tau (i_t - r - \pi_t) / \gamma - \mathcal{N}^{-1}(\alpha) \sqrt{\tau} \xi (V_t - s_t)$$

Need at least 3rd order approximation in discrete time

Optimal Monetary Policy Problem

Central bank solves

$$L = \min_{\{y_s, \pi_s, i_s\}} \mathbb{E}_t \int_t^\infty e^{-s\beta} (y_s^2 + \lambda \pi_s^2) ds$$

subject to

Dynamic IS:
$$dy_t = \frac{1}{\gamma} (i_t - r - \pi_t) dt + \xi (V_t - s_t) dZ_t$$

NKPC: $d\pi_t = (\beta \pi_t - \kappa y_t) dt$
Vulnerability: $V_t = -\tau \mathbb{E}_t [dy_t/dt] - \mathcal{N}^{-1}(\alpha) \sqrt{\tau} \operatorname{Vol}_t (dy_t/dt)$
Bank shocks: $ds_t = -\kappa (s_t - \overline{s}) + \sigma_s dZ_t$

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Augmented Taylor

$$i_t = \phi_0 + \phi_\pi \pi_t + \phi_y y_t + \phi_v V_t$$
$$= \Phi(V_t)$$

$$\pi_t = \psi_0 + \psi_y y_t + \psi_v V_t + \psi_s s_t$$

Coefficients φ and ψ are a function of structural parameters that govern vulnerability

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Risk-Taking Channel of Monetary Policy

- Fixed prices for simplicity $(\pi = 0)$
- Using the IS equation

$$dy_t = \frac{1}{\gamma} \left(i_t - r \right) dt + \xi \left(V_t - s_t \right) dZ_t$$

$$\mathbb{E}_t[dy_t/dt] = \frac{1}{\gamma}(i_t - r)$$
$$Vol_t(dy_t/dt) = \xi(V_t - s_t)$$

into

$$V_t = - au \mathbb{E}_t [dy_t/dt] - \mathcal{N}^{-1}(lpha) \sqrt{ au} \, extsf{Vol}_t (dy_t/dt)$$

to see that V_t and i_t are one-to-one: The *risk-taking channel* of monetary policy

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Output Gap Mean-Volatility Tradeoff

Eliminating i_t, dynamics of the economy are

$$dy_t = \xi \left(M V_t + \frac{\mathcal{N}^{-1}(\alpha)}{\sqrt{\tau}} s_t \right) dt + \xi \left(V_t - s_t \right) dZ_t$$

where

$$M \equiv -\frac{\xi + \mathcal{N}^{-1}(\alpha)\sqrt{\tau}}{\tau\xi}$$

is the slope of the mean-volatility line for output gap

$$\mathbb{E}_t \left[dy_t / dt
ight] = M \operatorname{Vol}_t \left(dy_t / dt
ight) - rac{1}{ au} s_t$$

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Recall Mean-Vol Line for Output Gap Growth



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Model Produces Mean-Vol Line for Output Gap Growth



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Model Produces Mean-Vol Line for Output Gap Growth



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Model Produces Mean-Vol Line for Output Gap Growth



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Calibration

- Use standard New Keynesian parameters when possible
- For parameters relating to vulnerability, match empirical and model-based regression of the conditional mean on the conditional vol of output gap growth
- Intercept, slope, standard deviation and AR(1) coefficient of residuals identify all new parameters

Interest Rate Response to Vulnerability



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Welfare Gains: Steady State Distribution of Output Gap



Conclusion

Conclusion

- The NK model can be augmented by
 - A financial sector that intermediates subject to a Value-at-Risk constraint
 - Shocks to financial sector
- Matches the stylized fact that conditional upper GDP quantiles are constant, while lower GDP quantiles move with financial conditions
- Mathematically tractable
- Optimal monetary policy always depends on vulnerability
 - Optimal monetary policy conditions on vulnerability
 - Vulnerability responds to monetary policy
 - LAW or clean up after crisis depending on vulnerability
 - Magnitudes are potentially large quantitatively